## 61A Lecture 34

November 21st, 2011

## Last week

## Last week

Distributed computing

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Distributed computing

- Client-server


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- Client-server
- Peer-to-peer


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- Client-server
- Peer-to-peer
- Message passing


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" Modularity


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- Client-server
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- Modularity
- Interfaces


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Parallel computing

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- Threads


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- Shared memory


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Distributed computing

- Client-server
- Peer-to-peer
- Message passing
- Modularity
- Interfaces

Parallel computing

- Threads
- Shared memory
- Problems: Synchronization and stale data


## Last week

Distributed computing

- Client-server
- Peer-to-peer
- Message passing
- Modularity
- Interfaces

Parallel computing

- Threads
- Shared memory
- Problems: Synchronization and stale data
- Solutions: Locks, semaphores (and conditions)


## Last week

Distributed computing

- Client-server
- Peer-to-peer
- Message passing
- Modularity
- Interfaces

Parallel computing

- Threads
- Shared memory
- Problems: Synchronization and stale data
- Solutions: Locks, semaphores (and conditions)
- Deadlock


## Sequential data

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Some of the most interesting real-world problems in computer science center around sequential data.

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DNA sequences

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DNA sequences
Web and cell-phone traffic streams

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The social data stream

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DNA sequences
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The social data stream
Series of measurements from instruments on a robot

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DNA sequences
Web and cell-phone traffic streams
The social data stream
Series of measurements from instruments on a robot
Stock prices, weather patterns

## So far: the sequence abstraction

## So far: the sequence abstraction

Sequences have

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Sequences have
Length

## So far: the sequence abstraction

Sequences have

- Length
- Element selection


## So far: the sequence abstraction

Sequences have

- Length
- Element selection
- In python


## So far: the sequence abstraction

Sequences have

- Length
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- Membership testing


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Data structures that support the sequence abstraction

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Data structures that support the sequence abstraction

- Nested tuples


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Data structures that support the sequence abstraction

- Nested tuples
- Tuples
- Strings


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Sequences have

- Length
- Element selection
- In python
- Membership testing
- Slicing

Data structures that support the sequence abstraction

- Nested tuples
- Tuples
- Strings
- Lists (mutable)


## Problems with sequences

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## Memory

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- Each item must be explicitly represented


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- Even if all can be generated by a common formula or function


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Can't be infinite
" Why care about "infinite" sequences?

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- Internet and cell phone traffic


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- Have to compute all items up-front
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- Instrument measurement feeds, real-time data


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Memory

- Each item must be explicitly represented
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- Have to compute all items up-front
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Can't be infinite

- Why care about "infinite" sequences?
- They're everywhere!
- Internet and cell phone traffic
- Instrument measurement feeds, real-time data
- Mathematical sequences


## Finding prime numbers

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Sieve of Erastothenes

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" Find prime numbers by walking down integers

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- Find prime numbers by walking down integers
- For each integer, eliminate all multiples of that integer


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## Finding prime numbers

Sieve of Erastothenes
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$=2345678910111213$
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## Working example: finding prime numbers

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Working example: finding prime numbers
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return primes
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                            1 billion
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1 billion
each number $=64$ bits $=8$ bytes

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return primes
                    primes_sieve(1000000000) anyone?
                        1 billion
                            each number = 64 bits = 8 bytes
8 bytes * 1 billion * 2 = 16 billion bytes
```

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            multiple = i*i
            while multiple <= limit :
            prime[multiple] = False
            multiple += i
return primes
                    primes_sieve(1000000000) anyone?
                        1 billion
                            each number = 64 bits = 8 bytes
8 bytes * 1 billion * 2 = 16 billion bytes
                        = ~14.9 GB of memory
```

Iterators: another abstraction for sequential data

# Iterators: another abstraction for sequential data 

Iterators

## Iterators: another abstraction for sequential data

Iterators

- Store how to compute items instead of items themselves


## Iterators: another abstraction for sequential data

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- Store how to compute items instead of items themselves
- Give out one item at a time


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- Save the next until asked (lazy evaluation)


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Compared with sequences

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- Length not explicitly defined


## Iterators: another abstraction for sequential data

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Compared with sequences

- Length not explicitly defined
- Element selection not supported


## Iterators: another abstraction for sequential data

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- Store how to compute items instead of items themselves
- Give out one item at a time
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- Length not explicitly defined
- Element selection not supported
- Element selection -- random access


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- Iterators -- sequential access
- No up-front computation of all items


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- Length not explicitly defined
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- Element selection -- random access
- Iterators -- sequential access
- No up-front computation of all items
- Only one item stored at a time


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- Store how to compute items instead of items themselves
- Give out one item at a time
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Compared with sequences

- Length not explicitly defined
- Element selection not supported
- Element selection -- random access
- Iterators -- sequential access
- No up-front computation of all items
- Only one item stored at a time
- CAN be infinite


## Implementation: nested delayed evaluation

## Implementation: nested delayed evaluation

Nested pairs


## Implementation: nested delayed evaluation

Nested pairs


Stream

## Implementation: nested delayed evaluation

Nested pairs


Stream


## Implementation: nested delayed evaluation

Nested pairs


Stream

first

## Implementation: nested delayed evaluation

Nested pairs


Stream


## Implementation: nested delayed evaluation

Nested pairs


Stream


## Implementation: nested delayed evaluation

Nested pairs


Stream


## Streams



## Streams

class Stream(object):


## Streams

class Stream(object):

def __init__(self, first, compute_rest, empty= False):

## Streams

class Stream(object):

def __init_(self, first, compute_rest, empty= False):

## Streams

class Stream(object):


$$
\begin{aligned}
& \text { def __init_(self, first, compute_rest, empty= False): } \\
& \text { self.first }=\text { first } \\
& \text { self._compute_rest }=\text { compute_rest }
\end{aligned}
$$

## Streams

class Stream(object):


$$
\begin{aligned}
& \text { def } \quad \text { _init__(self, first, compute_rest, empty= False): } \\
& \text { self.first }=\text { first } \\
& \text { self._compute_rest }=\text { compute_rest } \\
& \text { self.empty }=\text { empty }
\end{aligned}
$$

## Streams

class Stream(object):


```
def __init__(self, first, compute_rest, empty= False):
    self.first = first
    self._compute_rest = compute_rest
    self.empty = empty
    self._rest = None
```


## Streams

class Stream(object):


```
def __init__(self, first, compute_rest, empty= False):
    self.first = first
    self._compute_rest = compute_rest
    self.empty = empty
    self._rest = None
    self._computed = False
```


## Streams

class Stream(object):


```
def __init__(self, first, compute_rest, empty= False):
    self.first = first
    self._compute_rest = compute_rest
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    self._rest = None
    self._computed = False
```

@property

## Streams

class Stream(object):


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    self.first = first
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    self.empty = empty
    self._rest = None
    self._computed = False
@property
def rest(self):
```


## Streams

class Stream(object):


```
def __init__(self, first, compute_rest, empty= False):
    self.first = first
    self._compute_rest = compute_rest
    self.empty = empty
    self._rest = None
    self._computed = False
@property
def rest(self):
    assert not self.empty, 'Empty streams have no rest.'
```


## Streams

class Stream(object):


```
def __init__(self, first, compute_rest, empty= False):
    self.first = first
    self._compute_rest = compute_rest
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def rest(self):
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    if not self._computed:
```


## Streams

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    self.first = first
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@property
def rest(self):
    assert not self.empty, 'Empty streams have no rest.'
    if not self._computed:
        self._rest = self._compute_rest()
```


## Streams

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        self._computed = True
    return self._rest
```


## Streams

```
class Stream(object):
first
```

```
def __init__(self, first, compute_rest, empty= False):
```

def __init__(self, first, compute_rest, empty= False):
self.first = first
self.first = first
self._compute_rest = compute_rest
self._compute_rest = compute_rest
self.empty = empty
self.empty = empty
self._rest = None
self._rest = None
self._computed = False
self._computed = False
@property
def rest(self):
assert not self.empty, 'Empty streams have no rest.'
if not self._computed:
self._rest = self._compute_rest()
self._computed = True
return self._rest
empty_stream = Stream(None, None, True)

```


\section*{Sequential data: nested streams}

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Nest streams inside each other

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Nest streams inside each other Only compute one element of a sequence at a time

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Nest streams inside each other Only compute one element of a sequence at a time

def make_integer_stream(first=1):

\section*{Sequential data: nested streams}

Nest streams inside each other Only compute one element of a sequence at a time

def make_integer_stream(first=1):
def compute_rest():

\section*{Sequential data: nested streams}

Nest streams inside each other Only compute one element of a sequence at a time

def make_integer_stream(first=1):
def compute_rest():
return make_integer_stream(first+1)

\section*{Sequential data: nested streams}

Nest streams inside each other Only compute one element of a sequence at a time


\section*{Sequential data: nested streams}

Nest streams inside each other Only compute one element of a sequence at a time

def make_integer_stream(first=1):
def compute_rest(): return make_integer_stream(first+1)
return Stream(first, compute_rest)

\section*{Prime numbers with nested streams}

\section*{Prime numbers with nested streams}

\author{
def filter_stream(filter_func, stream):
}

\section*{Prime numbers with nested streams}

\author{
def filter_stream(filter_func, stream): def make_filtered_rest():
}

\section*{Prime numbers with nested streams}
```

def filter stream(filter func, stream):
def make_filtered_rest():
return filter_stream(filter_func, stream.rest)

```

\section*{Prime numbers with nested streams}
```

def filter_stream(filter_func, stream):
def make_filtered_rest():
return filter_stream(filter_func, stream.rest)
if stream.empty:

```

\section*{Prime numbers with nested streams}
```

def filter_stream(filter_func, stream):
def make_filtered_rest():
return filter_stream(filter_func, stream.rest)
if stream.empty:
return stream

```

\section*{Prime numbers with nested streams}
```

def filter stream(filter func, stream):
def make_filtered_rest():
return filter_stream(filter_func, stream.rest)
if stream.empty:
return stream
if filter_func(stream.first):

```

\section*{Prime numbers with nested streams}
```

def filter_stream(filter_func, stream):
def make_filtered_rest():
return filter_stream(filter_func, stream.rest)
if stream.empty:
return stream
if filter_func(stream.first):
return Stream(s.first, make_filtered_rest)

```

\section*{Prime numbers with nested streams}
```

def filter_stream(filter_func, stream):
def make_filtered_rest():
return filter_stream(filter_func, stream.rest)
if stream.empty:
return stream
if filter_func(stream.first):
return Stream(s.first, make_filtered_rest)
else:

```

\section*{Prime numbers with nested streams}
```

def filter_stream(filter_func, stream):
def make_filtered_rest():
return filter_stream(filter_func, stream.rest)
if stream.empty:
return stream
if filter_func(stream.first):
return Stream(s.first, make_filtered_rest)
else:
return filter_stream(filter_funct, stream.rest)

```

\section*{Prime numbers with nested streams}
```

def filter_stream(filter_func, stream):
def make_filtered_rest():
return filter_stream(filter_func, stream.rest)
if stream.empty:
return stream
if filter_func(stream.first):
return Stream(s.first, make_filtered_rest)
else:
return filter_stream(filter_funct, stream.rest)

```
def primes(positive_ints):

\section*{Prime numbers with nested streams}
```

def filter_stream(filter_func, stream):
def make_filtered_rest():
return filter_stream(filter_func, stream.rest)
if stream.empty:
return stream
if filter_func(stream.first):
return Stream(s.first, make_filtered_rest)
else:
return filter_stream(filter_funct, stream.rest)

```
def primes(positive_ints):
        def not_divible(x):

\section*{Prime numbers with nested streams}
```

def filter_stream(filter_func, stream):
def make_filtered_rest():
return filter_stream(filter_func, stream.rest)
if stream.empty:
return stream
if filter_func(stream.first):
return Stream(s.first, make_filtered_rest)
else:
return filter_stream(filter_funct, stream.rest)

```
def primes(positive_ints):
        def not_divible(x):
        return (x \% positive_integers.first) != 0

\section*{Prime numbers with nested streams}
```

def filter_stream(filter_func, stream):
def make_filtered_rest():
return filter_stream(filter_func, stream.rest)
if stream.empty:
return stream
if filter_func(stream.first):
return Stream(s.first, make_filtered_rest)
else:
return filter_stream(filter_funct, stream.rest)

```
def primes(positive_ints):
    def not_divible(x):
    return (x \% positive_integers.first) != 0
    def sieve():

\section*{Prime numbers with nested streams}
```

def filter_stream(filter_func, stream):
def make_filtered_rest():
return filter_stream(filter_func, stream.rest)
if stream.empty:
return stream
if filter_func(stream.first):
return Stream(s.first, make_filtered_rest)
else:
return filter_stream(filter_funct, stream.rest)

```
def primes(positive_ints):
    def not_divible(x):
    return (x \% positive_integers.first) != 0
    def sieve():
        return primes(filter_stream(not_divible, positive_ints.rest))

\section*{Prime numbers with nested streams}
```

def filter_stream(filter_func, stream):
def make_filtered_rest():
return filter_stream(filter_func, stream.rest)
if stream.empty:
return stream
if filter_func(stream.first):
return Stream(s.first, make_filtered_rest)
else:
return filter_stream(filter_funct, stream.rest)

```
def primes(positive_ints):
    def not_divible(x):
    return (x \% positive_integers.first) != 0
    def sieve():
        return primes(filter_stream(not_divible, positive_ints.rest))
    return Stream(pos_stream.first, sieve)

\section*{Prime numbers with nested streams}

\section*{Prime numbers with nested streams}
def primes(positive_ints):

\section*{Prime numbers with nested streams}
def primes(positive_ints):
def not_divible(x):

\section*{Prime numbers with nested streams}
```

def primes(positive_ints):
def not_divible(x):
return (x % positive_integers.first) != 0

```

\section*{Prime numbers with nested streams}
```

def primes(positive_ints):
def not_divible(x):
return (x % positive_integers.first) != 0
def sieve():

```

\section*{Prime numbers with nested streams}
def primes(positive_ints):
def not_divible(x):
return (x \% positive_integers.first) != 0
def sieve():
return primes(filter_stream(not_divible, positive_ints.rest

\section*{Prime numbers with nested streams}
def primes(positive_ints):
def not_divible(x):
return (x \% positive_integers.first) != 0
def sieve():
return primes(filter_stream(not_divible, positive_ints.rest return Stream(pos_stream.first, sieve)

\section*{Prime numbers with nested streams}
def primes(positive_ints):
def not_divible(x):
return (x \% positive_integers.first) != 0
def sieve():
return primes(filter_stream(not_divible, positive_ints.rest return Stream(pos_stream.first, sieve)
>>> p = primes(make_integer_stream(5))

\section*{Prime numbers with nested streams}

\section*{def primes(positive_ints):}
def not_divible(x):
return (x \% positive_integers.first) != 0
def sieve():
return primes(filter_stream(not_divible, positive_ints.rest return Stream(pos_stream.first, sieve)
>>> p = primes(make_integer_stream(5))
>>> p.first

\section*{Prime numbers with nested streams}
def primes(positive_ints):
def not_divible(x):
return (x \% positive_integers.first) != 0
def sieve():
return primes(filter_stream(not_divible, positive_ints.rest return Stream(pos_stream.first, sieve)
>>> p \(\neq\) primes(make_integer_stream(5))
>>> p.first

\section*{Prime numbers with nested streams}
```

def primes(positive_ints):
def not_divible(x):
return (x % positive_integers.first) != 0
def sieve():
return primes(filter_stream(not_divible, positive_ints.rest
return/Stream(pos_stream.first, sieve)
>>> p \# primes(make_integer_stream(5))
>>> p.first
5

```

\section*{Prime numbers with nested streams}
```

def primes(positive_ints):
def not_divible(x):
return (x % positive_integers.first) != 0
def sieve():
return primes(filter_stream(not_divible, positive_ints.rest
return Stream(pos_stream.first, sieve)
>>> p \# primes(make_integer_stream(5))
>>> p.first
5
>>> p.rest

```

\section*{Prime numbers with nested streams}
```

def primes(positive_ints):
def not_divible(x):
return (x % positive_integers.first) != 0
def sieve():
return primes(filter_stream(not_divible, positive_ints.rest
return Stream(pos_stream.first, sieve)
>>> p\# primes(make_integer_stream(5))
>>> p.first
5

```
```

>>> p.rest

```
```

>>> p.rest

```

\section*{Prime numbers with nested streams}
```

def primes(positive_ints):
def not_divible(x):
return (x % positive_integers.first) != 0
def sieve():
return primes(filter_stream(not_divible, positive_ints.rest
return Stream(pos_stream.first, sieve)
>>> p\not= primes(make_integer_stream(5))
>>> p.first
5
>>> p.rest
<Stream instance at ... >

```

\section*{Prime numbers with nested streams}
```

def primes(positive_ints):
def not_divible(x):
return (x % positive_integers.first) != 0
def sieve():
return primes(filter_stream(not_divible, positive_ints.rest
return Stream(pos_stream.first, sieve)
>>> p\# primes(make_integer_stream(5))
>>> p.first
5
>>> p.rest
<Stream instance at ... >
>>> p.rest.first

```

\section*{Prime numbers with nested streams}
```

def primes(positive_ints):
def not_divible(x):
return (x % positive_integers.first) != 0
def sieve():
return primes(filter_stream(not_divible, positive_ints.rest
return Stream(pos_stream.first, sieve)
>>> p\# primes(make_integer_stream(5))
>>> p.first
5
>>> p.rest
<Stream instance at ... >
>>> p.rest.first
7

```

\section*{Native python iterators}

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Python natively supports iterators

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Python natively supports iterators
The Iterator interface in python:

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Python natively supports iterators
The Iterator interface in python:
_ _iter_

\section*{Native python iterators}

Python natively supports iterators
The Iterator interface in python:
_ _iter__
- should return an iterator object

\section*{Native python iterators}

Python natively supports iterators
The Iterator interface in python:
"_iter_
- should return an iterator object
_ _next_

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Python natively supports iterators
The Iterator interface in python:
"_iter__
- should return an iterator object
_ _next__
- should return a value OR

\section*{Native python iterators}

Python natively supports iterators
The Iterator interface in python:
"_iter__
- should return an iterator object
_ _next__
- should return a value OR
- raise StopIteration

\section*{Native python iterators}

Python natively supports iterators
The Iterator interface in python:
\(\qquad\)
-should return an iterator object
" _next__
- should return a value OR
" raise StopIteration
-when end of sequence is reached

\section*{Native python iterators}

Python natively supports iterators
The Iterator interface in python:
\(\qquad\)
-should return an iterator object
" _next__
- should return a value OR
" raise StopIteration
- when end of sequence is reached
- on all subsequent calls

Native python iterators: example

Native python iterators: example class Letters(object):

Native python iterators: example class Letters(object): def __init__(self, start, finish):

Native python iterators: example class Letters(object):
def __init__(self, start, finish):
self.current = start

Native python iterators: example class Letters(object):
def __init__(self, start, finish):
self.current = start
self.finish = finish

Native python iterators: example class Letters(object):
def __init__(self, start, finish):
self.current = start
self.finish = finish
def __next__(self):

Native python iterators: example class Letters(object):
def __init__(self, start, finish):
self.current = start
self.finish = finish
def \(\overline{\text { if }}\) next_(self.current \(>\) self.finish:

Native python iterators: example class Letters(object):
```

def __init__(self, start, finish):
self.current = start
self.finish = finish

```
    def __next__(self):
    if self.current > self.finish:
                raise StopIteration

\section*{Native python iterators: example} class Letters(object):

\author{
def __init__(self, start, finish): \\ self.current = start \\ self.finish = finish \\ def __next__(self): \\ \(\overline{i f}\) self.current > self.finish: \\ raise StopIteration \\ result = self.current
}

\section*{Native python iterators: example} class Letters(object):

```

def __next__(self):
if self.current > self.finish:
raise StopIteration
result = self.current
self.current = chr(ord(result)+1)

```

\section*{Native python iterators: example} class Letters(object):

def __next__(self):
if self.current > self.finish: raise StopIteration result = self.current self.current \(=\operatorname{chr}(\operatorname{ord}(r e s u l t)+1)\) return result

\section*{Native python iterators: example} class Letters(object):
def \(\quad\) init__(self, start, finish):
self.current = start
self.finish \(=\) finish
```

def __next__(self):
if self.current > self.finish:
raise StopIteration
result = self.current
self.current = chr(ord(result)+1)
return result

```
    def __iter__(self):

\section*{Native python iterators: example} class Letters(object):
```

def __init__(self, start, finish):
self.current = start
self.finish = finish

```
    def __next__(self):
        \(\overline{\text { if }}\) self.current > self.finish:
                raise StopIteration
    result = self.current
    self.current = chr(ord(result)+1)
    return result
    def __iter__(self):
    return self

\section*{Native python iterators: example} class Letters(object):
def \(\quad\) init_(self, start, finish):
self.current = start
self.finish \(=\) finish
```

def __next__(self):
result = self.current
def __iter__(self):
return self

```
    \(\overline{\text { if }}\) self.current > self.finish:
                raise StopIteration
    self.current = chr(ord(result)+1)
    return result >>> letters = Letters('a', 'd')

\section*{Native python iterators: example} class Letters(object):
def \(\quad\) init_(self, start, finish):
self.current = start
self.finish \(=\) finish
```

def __next__(self):
if self.current > self.finish:
raise StopIteration
result = self.current
self.current = chr(ord(result)+1)
return result
>>> letters = Letters('a', 'd')
>>> letters.__next__()
def __iter__(self):
return self

```

\section*{Native python iterators: example} class Letters(object):
def \(\quad\) init_(self, start, finish):
self.current = start
self.finish \(=\) finish
```

def __next__(self):
if self.current > self.finish:
raise StopIteration
result = self.current
self.current = chr(ord(result)+1)
return result
>>> letters = Letters('a', 'd')
def __iter__(self):
return self

```

\section*{Native python iterators: example} class Letters(object):
def \(\quad\) init_(self, start, finish):
self.current = start
self.finish \(=\) finish
```

def __next__(self):
if self.current > self.finish:
raise StopIteration
result = self.current
self.current = chr(ord(result)+1)
return result
>>> letters = Letters('a', 'd')
def __iter__(self):
return self
>>> letters.__next__()
'a'
>>> letters.__next__()

```

\section*{Native python iterators: example} class Letters(object):
def \(\quad\) init_(self, start, finish):
self.current = start
self.finish \(=\) finish
```

def __next__(self):
if self.current > self.finish:
raise StopIteration
result = self.current
self.current = chr(ord(result)+1)
return result
def __iter__(self):
return self

```
```

>>> letters = Letters('a', 'd')

```
>>> letters = Letters('a', 'd')
>>> letters.__next__()
>>> letters.__next__()
'a'
'a'
>>> letters.__next__()
>>> letters.__next__()
'b'
```

'b'

```

\section*{Native python iterators: example} class Letters(object):
def \(\quad\) init_(self, start, finish):
self.current = start
self.finish \(=\) finish
```

def __next__(self):
if self.current > self.finish:
raise StopIteration
result = self.current
self.current = chr(ord(result)+1)
return result
def __iter__(self):
return self

```
```

>>> letters = Letters('a', 'd')

```
>>> letters = Letters('a', 'd')
>>> letters.__next__()
>>> letters.__next__()
'a'
'a'
>>> letters.__next__()
>>> letters.__next__()
'b'
'b'
>>> letters.__next__()
```

>>> letters.__next__()

```

\section*{Native python iterators: example} class Letters(object):
def \(\quad\) init_(self, start, finish):
self.current = start
self.finish \(=\) finish
```

def __next__(self):
if self.current > self.finish:
raise StopIteration
result = self.current
self.current = chr(ord(result)+1)
return result
def __iter__(self):
return self

```
```

>>> letters = Letters('a', 'd')

```
>>> letters = Letters('a', 'd')
```

>>> letters.__next__()

```
>>> letters.__next__()
'a'
'a'
>>> letters.__next__()
>>> letters.__next__()
'b'
'b'
>>> letters.__next__()
>>> letters.__next__()
'c'
```

'c'

```

\section*{Native python iterators: example} class Letters(object):
```

def __init__(self, start, finish):
self.current = start
self.finish = finish

```

>>> Letters = Letters( \(\left.a^{\prime}, d^{\prime}\right)\)
>>> letters.__next__()
'a'
>>> letters.__next__()
'b'
>>> letters.__next__()
'c'
>>> letters.__next__()

\section*{Native python iterators: example} class Letters(object):
```

def __init__(self, start, finish):
self.current = start
self.finish = finish

```

>>> Letters = Letters( \(\left.\mathrm{a}^{\prime}, \mathrm{d}^{\prime}\right)\)
>>> letters.__next__()
'a'
>>> letters.__next__()
'b'
>>> letters.__next__()
'c'
>>> letters.__next__()
'd'

\section*{Native python iterators: example} class Letters(object):
```

def __init__(self, start, finish):
self.current = start
self.finish = finish

```
```

def __next__(self):
result = self.current
return result
def __iter__(self):
return self

```
    \(\overline{\text { if }}\) self.current > self.finish:
                raise StopIteration
    self.current = chr(ord(result)+1)
```

>>> letters = Letters('a', 'd')
>>> letters.__next__()
'a'
>>> letters.__next__()
'b'
>>> letters.__next__()
'C'
>>> letters.__next__()
'd'
>>> letters.__next

```
\(\qquad\)

\section*{Native python iterators: example} class Letters(object):
```

def __init__(self, start, finish):
self.current = start
self.finish = finish

```
```

def __next__(self):
result = self.current
return result
def __iter__(self):
return self

```
    \(\overline{\text { if }}\) self.current > self.finish:
                raise StopIteration
    self.current = chr(ord(result)+1)
```

>>> letters = Letters('a', 'd')
>>> letters.__next__()
'a'
>>> letters.__next_()
'b'
>>> letters.__next__()
'c'
>>> letters.__next__()
'd'
>>> letters.__next__()
Traceback (m\overline{ost re\overline{cent call last):}}\mathbf{}\mathrm{ ( }
File "<stdin>", line 1, in <module>
File "<stdin>", line 12, in next
StopIteration

```

\section*{From a native python iterator to a nested stream}

\title{
From a native python iterator to a nested stream \\ empty_stream = Stream(None, None, True)
}

\section*{From a native python iterator to a nested stream}
```

empty_stream = Stream(None, None, True)
def iterator_to_stream(iterator):

```

\section*{From a native python iterator to a nested stream}
```

empty_stream = Stream(None, None, True)
def iterator_to_stream(iterator):
def streamify():

```

\section*{From a native python iterator to a nested stream}
```

empty_stream = Stream(None, None, True)
def iterator_to_stream(iterator):
def streamify():
try:

```

\section*{From a native python iterator to a nested stream}
```

empty_stream = Stream(None, None, True)
def iterator_to_stream(iterator):
def streamify():
try:
first = iterator.__next__()

```

\section*{From a native python iterator to a nested stream}
```

empty_stream = Stream(None, None, True)
def iterator_to_stream(iterator):
def streamify():
try:
first = iterator.__next__()
return Stream(first, streamify)

```

\section*{From a native python iterator to a nested stream}
```

empty_stream = Stream(None, None, True)
def iterator_to_stream(iterator):
def streamify():
try:
first = iterator.__next__()
return Stream(first, streamify)
except:

```

\section*{From a native python iterator to a nested stream}
```

empty_stream = Stream(None, None, True)
def iterator_to_stream(iterator):
def streamify():
try:
first = iterator.__next__()
return Stream(first, streamify)
except:
return empty_stream

```

\section*{From a native python iterator to a nested stream}
```

empty_stream = Stream(None, None, True)
def iterator_to_stream(iterator):
def streamify():
try:
first = iterator.__next__()
return Stream(first, streamify)
except:
return empty_stream
stream = streamify()

```

\section*{From a native python iterator to a nested stream}
```

empty_stream = Stream(None, None, True)
def iterator_to_stream(iterator):
def streamify():
try:
first = iterator.__next__()
return Stream(first, streamify)
except:
return empty_stream
stream = streamify()
return stream

```

\section*{More support: for loops!}

More support: for loops!
for item in obj:
do stuff

More support: for loops!
for item in obj:
do stuff
"for" loops use iterators

More support: for loops!
```

for item in obj:
do stuff
"for" loops use iterators

- Step 1: get an iterator

```

More support: for loops!

"for" loops use iterators
- Step 1: get an iterator
"iterator = obj.__iter

More support: for loops!
```

for item in obj: "for" loops use iterators
"Step 1: get an iterator
"iterator = obj.__iter
__()

- Step 2:

```

More support: for loops!
"for" loops use iterators
- Step 1: get an iterator
"iterator = obj.__iter \(\qquad\)
- Step 2:
" try iterator.__next__()

More support: for loops!
for item in obj: do stuff
"for" loops use iterators
- Step 1: get an iterator
-iterator = obj.__iter__()
- Step 2:
- try iterator.__next__()
- assign value to "item"

\section*{More support: for loops!}
for item in obj: do stuff
"for" loops use iterators
- Step 1: get an iterator
"iterator = obj.__iter \(\qquad\)
- Step 2:
- try iterator.__next__()
- assign value to "item"
- do body of loop

\section*{More support: for loops!}
for item in obj: do stuff
"for" loops use iterators
- Step 1: get an iterator
-iterator = obj.__iter__()
- Step 2:
- try iterator.__next__()
- assign value to "item"
- do body of loop
- until StopIteration is raised

\section*{More support: for loops!}
for item in obj: do stuff
"for" loops use iterators
- Step 1: get an iterator
"iterator = obj.__iter \(\qquad\)
- Step 2:
- try iterator.__next__()
- assign value to "item"
- do body of loop
- until StopIteration is raised
def for_each(sequence, function):

\section*{More support: for loops!}
for item in obj: do stuff
"for" loops use iterators
- Step 1: get an iterator
"iterator = obj.__iter \(\qquad\)
- Step 2:
- try iterator.__next__()
- assign value to "item"
- do body of loop
- until StopIteration is raised
def for_each(sequence, function): iterator = sequence.__iter__()

\section*{More support: for loops!}
for item in obj: do stuff
"for" loops use iterators
- Step 1: get an iterator
"iterator = obj.__iter \(\qquad\)
- Step 2:
- try iterator.__next__()
- assign value to "item"
- do body of loop
- until StopIteration is raised
def for_each(sequence, function): iterator = sequence.__iter__()
try:

\section*{More support: for loops!}
for item in obj: do stuff
"for" loops use iterators
- Step 1: get an iterator
"iterator = obj.__iter \(\qquad\)
- Step 2:
- try iterator.__next__()
- assign value to "item"
- do body of loop
- until StopIteration is raised
def for_each(sequence, function): iterator = sequence.__iter__()
try:
while True :

\section*{More support: for loops!}
for item in obj: do stuff
"for" loops use iterators
- Step 1: get an iterator
"iterator = obj.__iter \(\qquad\)
- Step 2:
- try iterator.__next__()
" assign value to "item"
- do body of loop
- until StopIteration is raised
def for_each(sequence, function): iterator = sequence.__iter__()
try:
while True :
element \(=\) iterator.__next__()

\section*{More support: for loops!}
for item in obj:
do stuff
"for" loops use iterators
- Step 1: get an iterator
"iterator = obj.__iter \(\qquad\)
- Step 2:
- try iterator.__next__()
- assign value to "item"
- do body of loop
- until StopIteration is raised
def for_each(sequence, function): iterator = sequence.__iter__()
try:
while True :
element = iterator.__next__() function(element)

\section*{More support: for loops!}

\section*{for item in obj: do stuff}

\section*{"for" loops use iterators}
- Step 1: get an iterator "iterator = obj.__iter \(\qquad\)
- Step 2:
" try iterator.__next__()
- assign value to "item"
- do body of loop
- until StopIteration is raised
def for_each(sequence, function):
iterator = sequence.__iter__()
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function(element)
except StopIteration as e:

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def for_each(sequence, function):
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pass

```

\section*{More support: for loops!}

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"for" loops use iterators
"Step 1: get an iterator
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```
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```


## Even more support: generator functions

## Even more support: generator functions

```
class Letters(object):
def __init__(self, start, finish):
    self.current = start
    self.finish = finish
    def __next__(self):
    if self.current > self.finish:
            raise StopIteration
        result = self.current
        self.current = chr(ord(result)+1)
        return result
    def __iter__(self):
    return self
```


## Even more support: generator functions

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    def __iter__(self): Generator version
        return self
    Generator version

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class Letters(object):
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    result = self.current
    self.current = chr(ord(result)+1)
    return result
```

    def __iter_(self): Generator version
    ```
def letters(start, finish):
    current = start
    while current <= finish:
    yield current
    current = chr(ord(current)+1)
```


## Even more support: generator functions

```
class Letters(object):
def __init__(self, start, finish):
    self.current = start
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    Generator version

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    def __iter_(self): Generator version
    def letters(start, finish):

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        result = self.current
    self.current = chr(ord(result)+1)
        return result
```

    def __iter__(self): Generator version
    return self
    
## Generator version

```
def letters(start, finish):
    current = start
```


## Even more support: generator functions

```
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    def __iter__(self): Generator version
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## Generator version

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def letters(start, finish):
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```


## Even more support: generator functions

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def __iter_(self): Generator version

```
def letters(start, finish):
    current = start
    while current <= finish:
    yield current
```


## Even more support: generator functions

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```


## Yield: a built-in flow-control statement

```
def letters(start, finish):
    current = start
    while current <= finish:
    yield current
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```


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Generator function. When called, creates a Generator object

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>>> l = letters('a', 'd')

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```
>>> l = letters('a', 'd')
```

>>> l

## Yield: a built-in flow-control statement

```
def letters(start, finish):
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            current = chr(ord(current)+1)
```

Generator function. When called, creates a Generator object

```
>>> l = letters('a', 'd')
>>> l
<generator instance at..>
```


## Yield: a built-in flow-control statement

```
```

def letters(start, finish):

```
```

def letters(start, finish):
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while current <= finish:
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yield current
current = chr(ord(current)+1)

```
```

        current = chr(ord(current)+1)
    ```
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## Yield: a built-in flow-control statement

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Generator function. When called, creates a Generator object
>>> l = letters('a', 'd')
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<generator instance at..>
Automatically creates:
l.__iter__()

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```
def letters(start, finish):
```

def letters(start, finish):
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current = start
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yield current
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<generator instance at..>
Automatically creates:
l.__iter__()
l.__next__()

## Yield: a built-in flow-control statement

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def letters(start, finish):
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when __next__() is called, starts

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when __next__() is called, starts
Goes through executing body of function

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Pauses at "yield" -- returns value

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Pauses at "yield" -- returns value
All local state is preserved

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>>> l = letters('a', 'd') >>> l
<generator instance at..>
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l.__next__()

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Iterators get used up

## Iterators get used up

>>> letters = Letters('a', 'd')

## Iterators get used up

>>> letters = Letters('a', 'd')
>>> letters.__next__()

```
Iterators get used up
>>> letters = Letters('a', 'd')
>>> letters.__next_()
a'
```

```
Iterators get used up
>>> letters = Letters('a', 'd')
>>> letters.__next_()
'a'
>>> letters.__next
()
```


## Iterators get used up

```
>>> letters = Letters('a', 'd')
>>> letters.__next__()
'a'
>>> letters.__next
'b'
```


## Iterators get used up

```
>>> letters = Letters('a', 'd')
>>> letters.__next__()
'a'
>>> letters.__next__()
'b'
>>> letters.__next__()
```


## Iterators get used up

```
>>> letters = Letters('a', 'd')
>>> letters.__next__()
'a'
>>> letters.__next__()
'b'
>>> letters.__next__()
'c'
```


## Iterators get used up

```
>>> letters = Letters('a', 'd')
>>> letters.__next__()
'a'
>>> letters.__next__()
'b'
>>> letters.__next__()
'c'
>>> letters.__next__()
```


## Iterators get used up

```
>>> letters = Letters('a', 'd')
>>> letters.__next__()
'a'
>>> letters.__next__()
'b'
>>> letters.__next__()
'c'
>>> letters.__next__()
'd'
```


## Iterators get used up

```
>>> letters = Letters('a', 'd')
>>> letters.__next__()
'a'
>>> letters.__next__()
'b'
>>> letters.__next__()
'c'
>>> letters.__next__()
'd'
>>> letters.__next
```

$\qquad$

```
Iterators get used up
>>> letters = Letters('a', 'd')
>>> letters.__next__()
'a'
>>> letters.__next__()
'b'
>>> letters.__next__()
'c'
>>> letters.__next__()
'd '
>>> letters.__next__()
Traceback (m\overline{os}t re\overline{cent call last):}
    File "<stdin>", line 1, in <module>
    File "<stdin>", line 12, in next
StopIteration
```


## Iterators get used up

```
>>> letters = Letters('a', 'd') The Iterator interface in python:
>>> letters.__next__()
'a'
>>> letters.__next__()
'b'
>>> letters.__next__()
'c'
>>> letters.__next__()
'd '
>>> letters.__next__()
Traceback (m\overline{os}t re\overline{cent call last):}
    File "<stdin>", line 1, in <module>
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The Iterator interface in python:
```

$\qquad$

```
- should return an iterator object
_ _next__
- should return a value OR
- raise StopIteration
- when end of sequence is reached
-on all subsequent calls
```

```

```


## Iterators get used up

```
>>> letters = Letters('a', 'd') The Iterator interface in python:
>>> letters.__next__()
'a'
>>> letters.__next__()
'b'
>>> letters.
'c'
>>> letters.
```



```
    File "<stdin>", line 1, in <module>
    File "<stdin>", line 12, in next
StopIteration
>>> letters
```

$\qquad$ next $\qquad$()
$\qquad$ next $\qquad$()
$\qquad$ next $\qquad$ ()

The Iterator interface in python:
$\qquad$
-should return an iterator object
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File "<stdin>", line 12, in next
StopIteration
>>> letters next

## Iterators get used up

```
>>> letters = Letters('a', 'd') The Iterator interface in python:
>>> letters.__next__()
'a'
>>> letters.__next__()
'b'
>>> letters
```

$\qquad$

``` next
``` \(\qquad\)
```()
'c'
>>> letters.__next__()
'd '
>>> letters.__next
Traceback (m\overline{os}t re\overline{cent call last):}
    File "<stdin>", line 1, in <module>
    File "<stdin>", line 12, in next
StopIteration
>>> letters
```

$\qquad$

``` next
``` \(\qquad\)
```

Traceback (most recent call last):
File "<stdin>", line 1, in <module>
File "<stdin>", line 12, in next
StopIteration

```
- __iter__
- should return an iterator object
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- should return a value OR
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- when end of sequence is reached
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\section*{Iterators get used up}
```

>>> letters = Letters('a', 'd') The Iterator interface in python:
>>> letters.

```
\(\qquad\)
``` next
``` \(\qquad\)
``` ()
'a'
>>> letters.__next__()
'b'
>>> letters.
```

$\qquad$

``` next
``` \(\qquad\)
```()
'c'
>>> letters.__next__()
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Traceback (m\overline{ost re\overline{cent call last):}}\mathbf{}\mathrm{ ( }
    File "<stdin>", line 1, in <module>
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StopIteration
>>> letters
```

$\qquad$

``` next
``` \(\qquad\)
``` ()
Traceback (most recent call last):
    File "<stdin>", line 1, in <module>
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StopIteration
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```

$\qquad$

``` next
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```

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File "<stdin>", line 12, in next StopIteration
>>> letters os recen
call last):
File "<stdin>", line 1, in <module> File "<stdin>", line 12, in next
StopIteration
>>> letters. _
```

$\qquad$

## Iterators get used up

```
>>> letters = Letters('a', 'd') The Iterator interface in python:
>>> letters.__next__()
'a'
>>> letters.__next__()
'b'
>>> letters.__next__()
'c'
>>> letters.__next__()
'd '
>>> letters._next__()
Traceback (m\overline{os}t re\overline{cent call last):}
    File "<stdin>", line 1, in <module>
    File "<stdin>", line 12, in next
StopIteration
>>> letters
```

$\qquad$

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Traceback (most recent call last):
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```
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StopIteration
```

Iterables -- new iterator for every __iter__()

## Iterables -- new iterator for every

$\qquad$ iter

```
class Letters(object):
```

    def __init__(self, start, finish):
        self.current = start
        self.finish = finish
    def __next__(self):
        if self.current > self.finish:
                raise StopIteration
        result = self.current
        self.current \(=\operatorname{chr}(\operatorname{ord}(\) result \()+1)\)
        return result
    def __iter__(self):
        return self
    
## Iterables -- new iterator for every

$\square$ iter _()

```
class Letters(object): class LetterSequence(object):
    def __init__(self, start, finish):
        self.current = start
        self.finish = finish
    def __next__(self):
        if self.current > self.finish:
                raise StopIteration
        result = self.current
        self.current = chr(ord(result)+1)
        return result
    def __iter__(self):
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```


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```


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## Iterables -- new iterator for every

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        return result
```

    def __iter__(self):
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## Iterables -- new iterator for every

$\qquad$ __()

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class Letters(object): class LetterSequence(object):
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                raise StopIteration
        result = self.current
        self.current = chr(ord(result)+1)
        return result
    def __iter__(self):
        return self
```

```
def __init__(self, start, finish):
```

def __init__(self, start, finish):
self.start = start
self.start = start
self.finish = finish
self.finish = finish
def __iter__(self):
def __iter__(self):
return self.forward()
return self.forward()
def forward(self):
def forward(self):
current = self.start
current = self.start
if current < self.finish:
if current < self.finish:
yield current

```
    yield current
```


## Iterables -- new iterator for every

$\qquad$ __()

```
class Letters(object): class LetterSequence(object):
    def __init__(self, start, finish):
        self.current = start
        self.finish = finish
    def __next__(self):
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                raise StopIteration
        result = self.current
        self.current = chr(ord(result)+1)
        return result
    def __iter__(self):
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```

```
def __init__(self, start, finish):
```

def __init__(self, start, finish):
self.start = start
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self.finish = finish
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def __iter__(self):
def __iter__(self):
return self.forward()
return self.forward()
def forward(self):
def forward(self):
current = self.start
current = self.start
if current < self.finish:
if current < self.finish:
yield current
yield current
current = chr(ord(current)+1)

```
    current = chr(ord(current)+1)
```


## Iterables -- new iterator for every

$\qquad$ iter _()

```
class Letters(object): class LetterSequence(object):
        def __init__(self, start, finish):
        self.current = start
        self.finish = finish
    def _next__(self):
    def __iter__(self):
        return self
def __iter__(self):1)
    def forward(self):
        current = self.start
        if current < self.finish:
        yield current
        current = chr(ord(current)+1)
            def __init__(self, start, finish):
        self.start = start
                                self.finish = finish
a generator function
```


## Iterables -- new iterator for every

$\qquad$ iter __()

```
class Letters(object):
    def __init__(self, start, finish):
        self.current = start
        self.finish = finish
    def _ _next__(self): 
    def __next__(self):
    def __next__(self):
    def __next__(self):
    def __next__(self): 
    def __next__(self):
    def __iter__(self):
        return self
```

                class LetterSequence(object):
            def __init__(self, start, finish):
        self.start = start
                                self.finish = finish
    def _iter_(self):
return(self.forward()
def forward(self):
current = self.start
if current < self.finish:
yield current
current $=$ chr(ord(cyrrent) +1)
a generator function
a new generator object every time

## Iterables -- new iterator for every

$\qquad$ iter _()

```
class Letters(object):
    def __init__(self, start, finish):
        self.current = start
        self.finish = finish
    def __next__(self):
    def __next__(self):
    def __next__(self):
    def __next__(self):
    def __next__(self): 
    def __next__(self):
    def __iter__(self):
        return self
```

                class LetterSequence(object):
            def __init__(self, start, finish):
        self.start = start
                                self.finish = finish
    def _iter_(self):
return(self.forward()
def forward(self):
current = self.start
if curent < self.finish:
yield current
current = chr(ord(cyrrent)+1)
a generator function
a new generator object every time

Any questions?

# Processing pipelines for sequential data 

Next time

