

Iterators

An iterator is an abstract object that represents a sequence of values. An iterator understands how to do two things. First of all, it knows how to calculate its next value, and hence can continuously output a stream of its values. Secondly, an iterator should know when it has no more values left to compute. We can see these two behaviors being exhibited in Python's iterator interface. Python's iterator interface has a `__next__` method that computes the next value in the sequence given the iterator's current state. When there are no more values left to compute, the `__next__` method is required to raise a `StopIteration` Exception, thus signalling the end of the value sequence.

The `__iter__` method is another method required by Python's iterator interface, and it merely returns the iterator object itself. In other words, calling `__iter__` returns an object that implements the `__next__` method.

Keep in mind that iterators are stateful objects and always keep track of how much of the stream has already been computed. Once an iterator invokes its `__next__` method, the calculated value gets “used-up” and thrown away, hence changing the iterator's state. If we then make another call to `__next__`, the returned value will be different from the previously calculated value.

Here is an example of a class that implements Python's iterator interface. This iterator calculates all of the natural numbers one-by-one, starting from zero:

```
class Naturals():
    def __init__(self):
        self.current = 0

    def __next__(self):
        result = self.current
        self.current += 1
        return result

    def __iter__(self):
        return self
```

Notice that the `__next__` method in `Naturals` never raises a `StopIteration` exception. Wait, but I thought iterators have to raise a `StopIteration` exception when they compute all of their values! Exactly, but it doesn't make sense to “compute the last natural number”, as the set of

natural numbers is infinitely large. Hence, we see here that iterators are perfectly capable of representing an infinite data stream using a finite amount of memory.

Also note that because the return statement must be the last one executed in the `__next__` method, we have to save the return value in a temporary variable, or else it would get overwritten by the intervening update step. Later on we will introduce python's `yield` statement, which lets you define iterators without worrying about saving the current state of the computation.

Questions

1. Define an iterator whose *i*-th element is the result of combining the *i*-th elements of two input streams using some binary operator, also given as input. The resulting iterator should have a size equal to the size of the shorter of its two input iterators.

```
>>> from operator import add
>>> evens = Iter_Combiner(Naturals(), Naturals(), add)
>>> evens.__next__()
0
>>> evens.__next__()
2
>>> evens.__next__()
4
```

```
class Iter_Combiner():
    def __init__(self, iter1, iter2, combiner):
```

```
        def __next__(self):
```

```
            def __iter__(self):
                return self
```

2. Create an iterator (using previously defined iterators) that represents the sequence of perfect squares.

3. What results from executing this sequence of commands?

```
>>> from operator import add
>>> naturals = Naturals()
>>> doubled_naturals = Iter_Combiner(naturals, naturals, add)
>>> doubled_naturals.__next__()
_____
>>> doubled_naturals.__next__()
_____
```

4. Create an iterator that generates the sequence of Fibonacci numbers.

```
class Fibonacci_Numbers():
    def __init__(self):
```

```
        def __next__(self):
```

```
            def __iter__(self):
                return self
```

Generators

A generator is a special kind of Python iterator that uses a yield statement instead of a return statement to report values. A yield statement is similar to a return statement, but whereas a return statement causes the current environment to be destroyed after a function exits, a yield statement inside a function causes the environment to be saved until the next time `__next__` is called, which allows the generator to keep track of the iteration state. Once `__next__` is called again, execution picks up from where the previously executed yield statement left off, and continues until the next yield statement is encountered.

Including a yield statement in a function automatically signals to Python that this function will create a generator. In other words, when we call the function, it will return a generator object, instead of executing the code inside the body. When the returned generator's `__next__` method is called, the code in the body is executed for the first time, and stops executing upon reaching the first yield statement.

A python function can either use return statements or yield statements in the body to output values, but not both. If the function has a single yield statement, then python treats the function as a generator, and will raise an error if the body also contains a return expression that outputs a value.

Here is an iterator for the natural numbers written using the generator construct:

```
def generate_naturals():
    current = 0
    while True:
        yield current
        current += 1
```

Questions

1. In this problem we will represent a set using a python list. Write a generator function that returns lists of all subsets of the positive integers from 1 to n. Each call to this generator's `__next__` method will return a list of subsets of the set $[1, 2, \dots, n]$, where n is the number of times `__next__` was previously called.

```
>>> subsets = generate_subsets()
>>> subsets.__next__()
[[]]
>>> subsets.__next__()
[[], [1]]
```

```
>>> subsets.__next__()
[[], [1], [2], [1, 2]]

def generate_subsets():
```

Streams

A stream is an element and a “promise” to evaluate the rest of the stream. You’ve already seen multiple examples of this and its syntax in lecture and in the book, so I will not dwell on that. Suffice it to say, streams is one of the most mysterious topics in CS61A, but it’s also one of the coolest; mysterious, because defining a stream often seems like black magic (and requires MUCH more trust than whatever trust you worked up for recursion); cool, because things like infinite streams allows you to store an INFINITE amount of data in a FINITE amount of space/time!

Examine the following code from lecture:

```
class Stream(object):
    def __init__(self, first, compute_rest, empty= False):
        self.first = first
        self._compute_rest = compute_rest
        self.empty = empty
        self._rest = None
        self._computed = False

    @property
    def rest(self):
        assert not self.empty, 'Empty streams have no rest.'
        if not self._computed:
            self._rest = self._compute_rest()
            self._computed = True
        return self._rest

empty_stream = Stream(None, None, True)
```

We represent Streams as Objects, and we represent a full Stream as nested Stream Objects. We nest streams inside one another, and compute one element of a sequence at a time. Notice also that streams are memoized. The first time a stream's rest() method is called, it computes the rest value, stores it, and returns it. After that, every time the method is called, the stored value is simply returned, it is not computed again.

Here is an Example:

```
def make_integer_stream(first=1):
    def compute_rest():
        return make_integer_stream(first+1)
    return Stream(first, compute_rest)
```

Notice what is happening here. We start out with a stream whose first element is 1, and whose compute_rest function creates another stream. So when we do compute the rest, we get another stream whose first element is the previous element + 1, and whose compute_rest creates another stream. So we effectively get an infinite stream of integers, computed one at a time. This is almost like an infinite recursion, but one which can be viewed one step at a time, and so does not crash.

Questions:

1. Write a procedure make_ones_stream() that creates an infinite stream of ones.

```
def make_ones_stream():
```

2. Write a procedure add_streams that takes in two streams as argument, and returns the Stream of each element of the two streams added together. Add the first element of each Stream, the second element of each Stream, and so on...You can assume that both Streams are infinite.

```
def add_streams(stream1, stream2):
```

3. Write a procedure `make_fib_stream()` that creates an infinite stream of Fibonacci Numbers. Make the first two elements of the stream 0 and 1.

Hint: Consider using a helper procedure that can take two arguments, then think about how to start calling that procedure.

```
def make_fib_stream()
```

Higher Order Functions on Streams:

Naturally, as the theme has always been in this class, we can abstract our stream procedures to be higher order. Take a look at `filter_stream` from lecture:

```
def filter_stream(filter_func, stream):  
    def make_filtered_rest():  
        return filter_stream(filter_func, stream.rest)  
    if stream.empty:  
        return stream  
    if filter_func(stream.first):  
        return Stream(s.first, make_filtered_rest)  
    else:  
        return filter_stream(filter_func, stream.rest)
```

You can see how this function might be useful. Notice how the Stream we create has as its `compute_rest` function a procedure that “promises” to filter out the rest of the Stream when asked. So at any one point, the entire stream has not been filtered. Instead, only the part of the stream that has been referenced has been filtered, but the rest will be filtered when asked. We can model other higher order Stream procedures after this one, and we can combine our higher order Stream procedures to do incredible things!

Questions:

1. In a similar model to `filter_stream`, write a procedure `map_stream`, that takes in a one-argument function, and does the obvious thing.

```
def stream_map(func, stream):
```

2. The following procedure when called creates a Stream. Given endless subsequent calls to the Stream to compute all its values, what are the values of the Stream created by the call to `my_stream()`. Don't write them all, just write enough to get the pattern.

```
def my_stream():
    def compute_rest():
        return add_streams(map_stream(double, my_stream()), my_stream())
    return Stream(1, compute_rest)
```